

# Financially-constrained firms and technological development: an Agent-Based Model

TESI PER LA CERTIFICAZIONE FINALE DELLA  
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# Motivation

- **Technological development** is the main driver of growth
- **Financial stability** affects output
- Key fact: only financially robust firms perform innovation
- Feedback between financial conditions of the market and technological development
- Make a simple **Agent-Based Model** to explore it

# Why interdisciplinary?

- Economy as a **complex system**
- Collection of entities whose collective behavior cannot be directly inferred from the individual behavior
- Anderson (1972)
- **Complexity economics**: bounded rationality, heterogeneity, out-of-equilibrium, interactions
- An example: Agent-Based Models

# Related literature

- **Endogenous growth**: Romer (1990), Aghion and Howitt (1992), Grossman and Helpman (1991), Dosi et al. (2010).

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- **Financial accelerator**: Greenwald and Stiglitz (1993), Bernanke et al. (1996), Delli Gatti et al. (2005, 2010, 2012)

# Overview

- Model
- No tech development
- Switching on tech development

# Production and costs

- $N$  firms denoted by  $i$ ; time  $t$ , discrete
- Equity (net worth, own capital)
- Planned quantity:
- Technology      capital
- Production function
- Perfect credit markets
- Costs:

# Production and costs

- $N$  firms denoted by  $i$ ; time  $t$ , discrete
- Equity (net worth, own capital):  $A(i, t)$
- **Planned quantity:**  $\tilde{Q}(i, t) = \alpha A(i, t)^\beta > 0$
- Technology  $\gamma(i, t)$ , capital  $K(i, t)$
- **Production function:**  $Q(i, t) = (\gamma(i, t)K(i, t))^\delta$
- Perfect credit markets:  $Q(i, t) \equiv \tilde{Q}(i, t)$

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- Perfect credit markets:  $Q(i, t) \equiv \tilde{Q}(i, t)$
- **Costs:**  $C(i, t) = gK(i, t) + RD(i, t)$

# Market mechanism

- Selling price:  $P(i, t) = u(i, t)P(t - 1)$

• Nominal revenues:

• Profits:

• Update:

# Market mechanism

- Selling price:  $P(i, t) = u(i, t)P(t - 1)$
- Nominal revenues:  $Y(i, t) = P(i, t)Q(i, t)$
- Profits:  $\Pi(i, t) = Y(i, t) - C(i, t)$
- Update:  $A(i, t + 1) = A(i, t) + \Pi(i, t)$

# Technological development

- **States:** robust (RB), fragile (FR), bankrupt

$$\mathbb{P}\{A(i, t+1) < 0\} = \mathbb{P}\{A(i, t) + \Pi(i, t) < 0\}$$

# Technological development

- States: robust (RB), fragile (FR), bankrupt

$$\mathbb{P}\{A(i, t+1) < 0\} = \mathbb{P}\{A(i, t) + \Pi(i, t) < 0\}$$

- RB firms spend fraction  $v$  of revenues on R&D
- **Innovation:**  $\gamma(i, t+1) = (1 + \zeta(rd(i, t)))\gamma(i, t)$
- FR firms engage in **imitation**

# Wrap-up

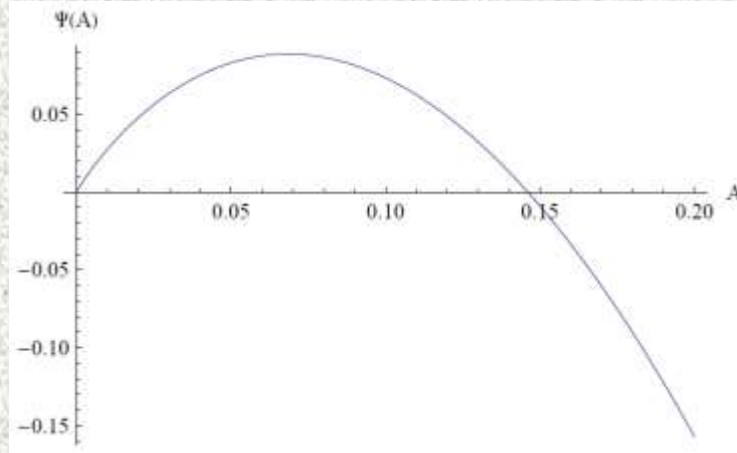
- Production financially constrained
- Stylized market mechanism with shocks
- State update
- Innovation and imitation
- Exit and entry

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# Baseline case

- Fixed technology:  $\gamma(i, t) = \gamma$
- Constant price:  $P(t) = P$
- Deterministic dynamics:  $u(i, t) = 1$

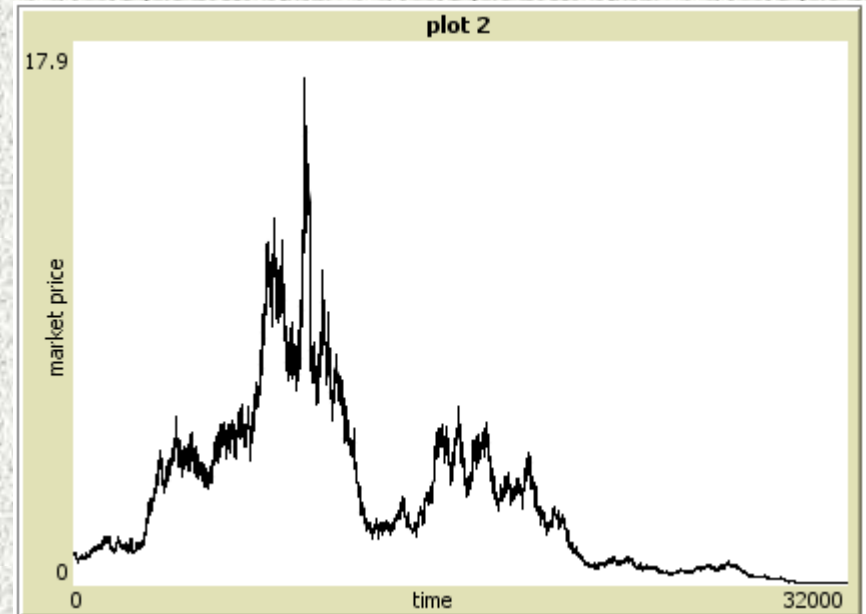
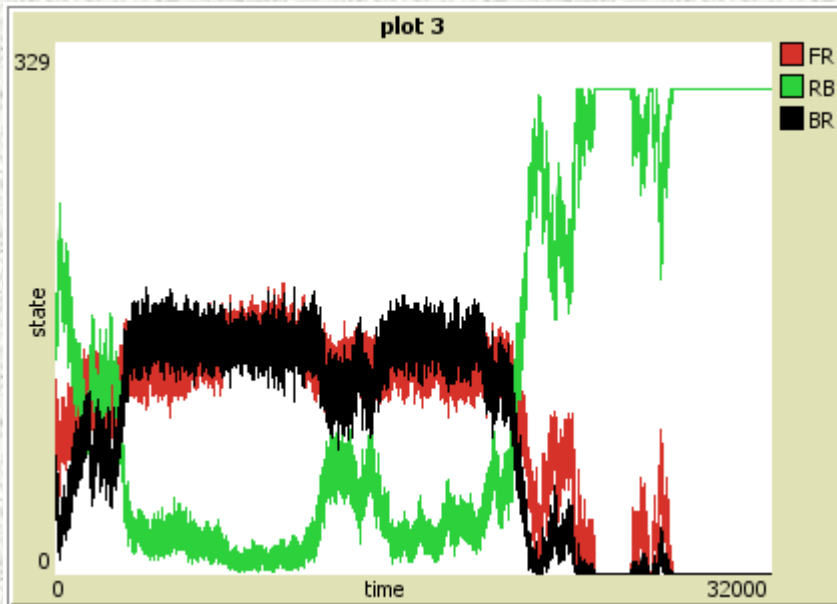


$$A^* = \left[ \frac{\gamma P}{g} \alpha^{1-1/\delta} \right]^{\frac{\delta}{\delta-\beta}}$$

$$\Psi(A_{RB}) = 1 + u_0 P \alpha A_{RB}^{\beta-1} - \frac{g \alpha^{1/\delta}}{\gamma} A_{RB}^{\beta/\delta-1} = 0$$



# Price evolution



# Overview

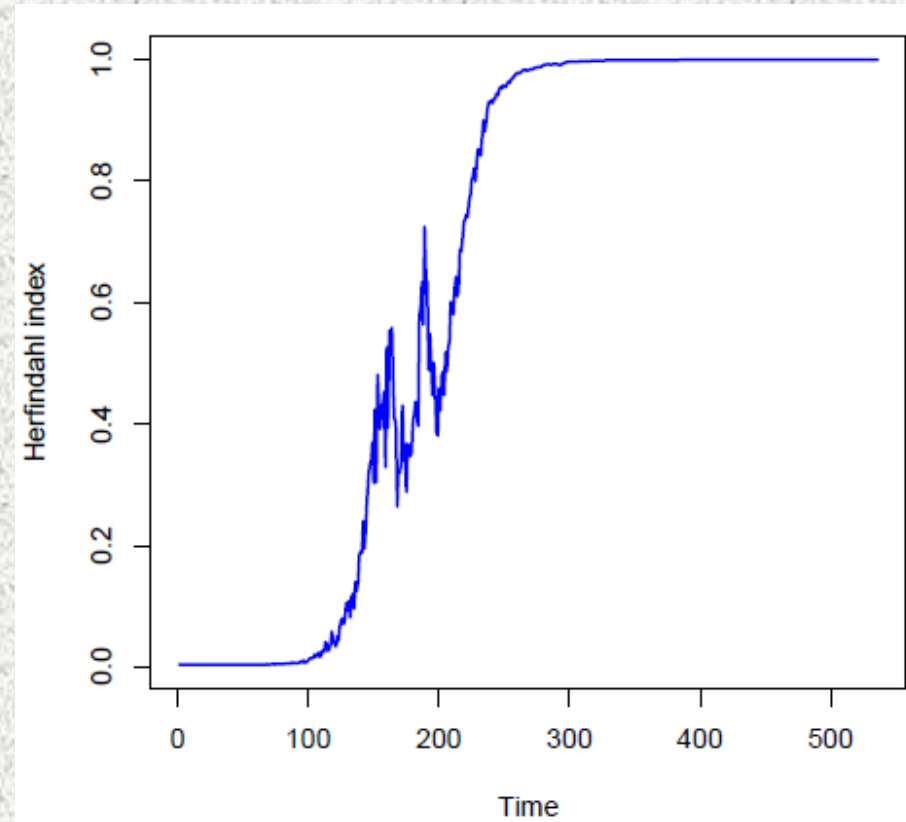
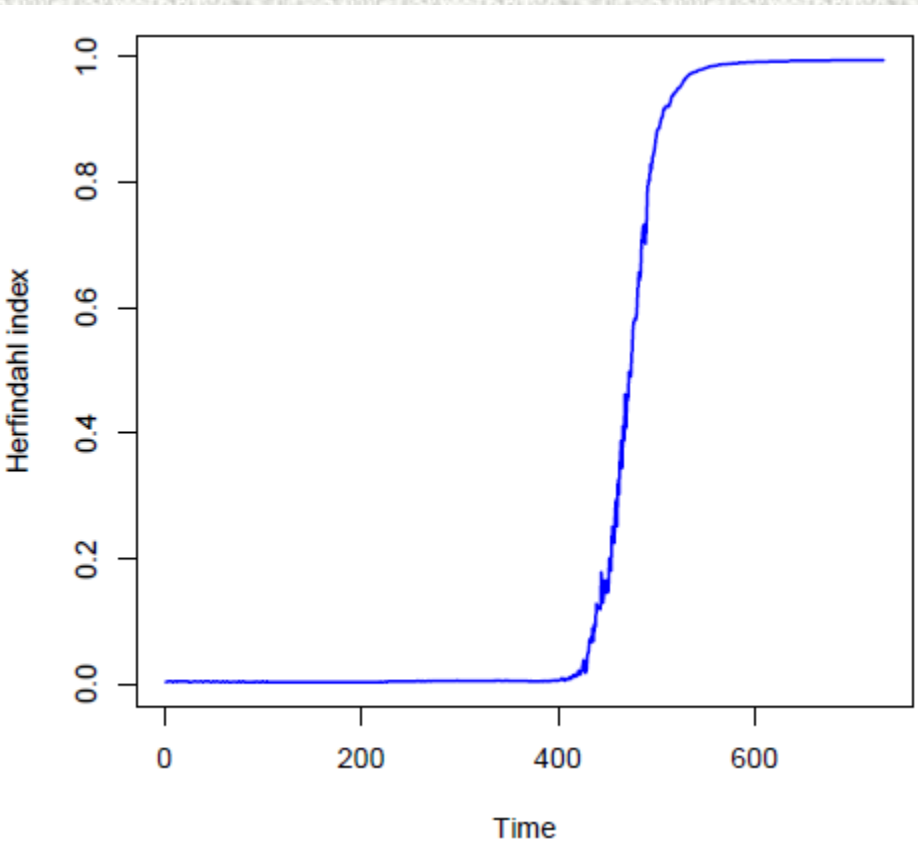
- Model
- No tech development
- **Switching on tech development**

# Relevant quantities

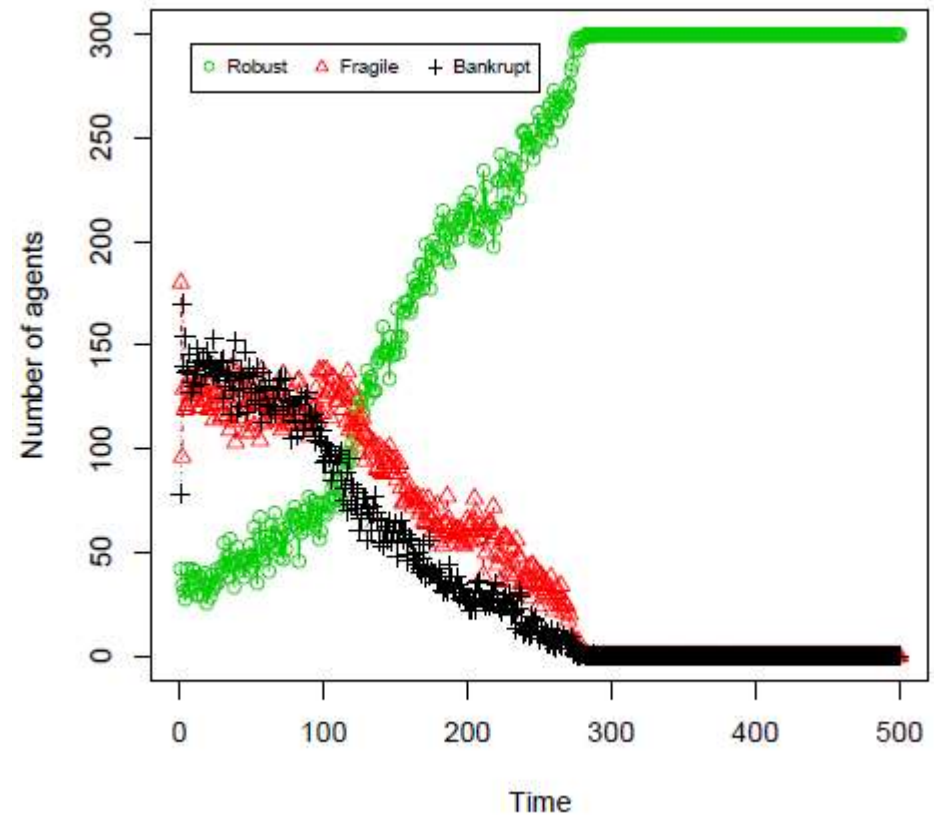
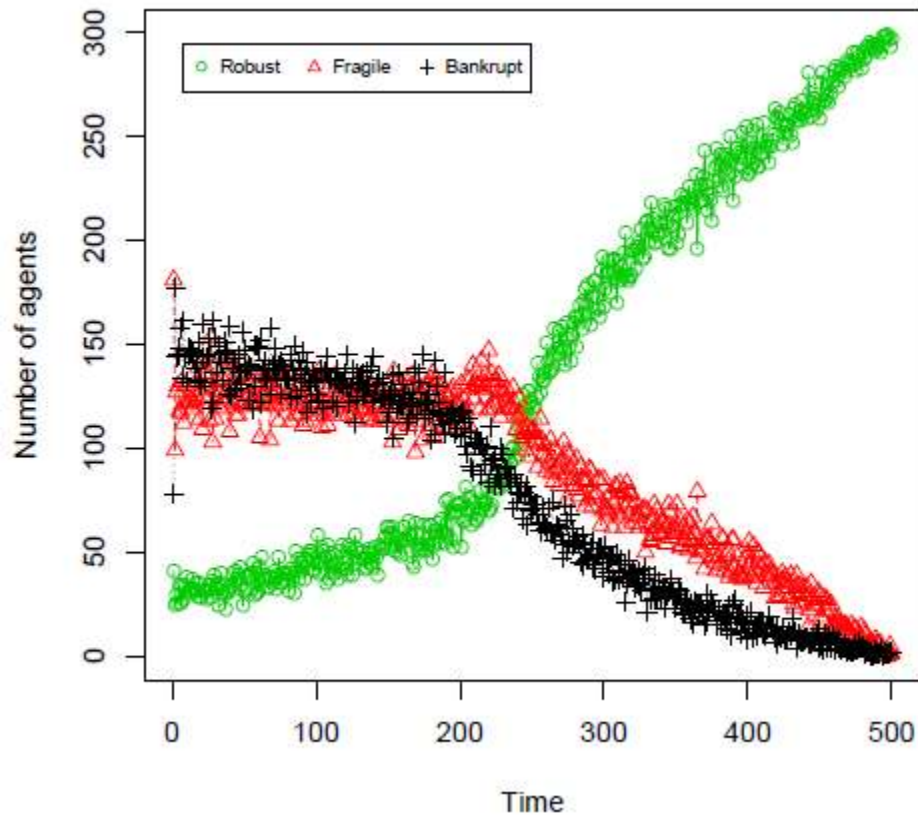
- Feedback effects between the credit constraints and the interplay between innovation and imitation.
- **Prevalent state**: RB or FR
- **Herfindhal index**:

$$H = \sum_{i=1}^N s_i^2, \quad s_i = \frac{Q(i, t)}{Q(t)}$$

# RB markets become concentrated sooner



# Concentrated markets become RB later



# Conclusions

- Technological development makes the market (more) robust
- Ceteris paribus, a robust market with technological development becomes concentrated sooner
- Ceteris paribus, a market where innovation is more common than imitation becomes robust sooner

# Thank you for your attention!

